

UPPER AND LOWER WEAKLY LPT m - I -CONTINUOUS MULTIFUNCTIONS

TAKASHI NOIRI¹ AND VALERIU POPA²

ABSTRACT. In this paper, by using the m -structure $mIO(X)$ constructed by the topology τ and the ideal I in an ideal topological space (X, τ, I) , we define upper/lower weakly LPT m - I -continuous multifunctions and establish their properties, where LPT denotes one of nearly compact, compact, Lindelöf, and connected sets.

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¹ 2949-1 SHIOKITA-CHO, HINAGU, YATSUSHIRO-SHI, KUMAMOTO-KEN, 869-5142 JAPAN

² DEPARTMENT OF MATHEMATICS AND INFORMATICS, "VASILE ALECSANDRI" UNIVERSITY OF BACĂU, CALEA MARASESTI 157, BACĂU, 600115. ROMANIA

Email address: ¹ t.noiri@nifty.com, ² vpopa@ub.ro